

# THE MICROSOFT 2016 CONVERSATIONAL SPEECH RECOGNITION SYSTEM

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## ABSTRACT

We describe Microsoft’s conversational speech recognition system, in which we combine recent developments in neural-network-based acoustic and language modeling to advance the state of the art on the Switchboard recognition task. Inspired by machine learning ensemble techniques, the system uses a range of convolutional and recurrent neural networks. I-vector modeling and lattice-free MMI training provide significant gains for all acoustic model architectures. Language model rescoring with multiple forward and backward running RNNLMs, and word posterior-based system combination provide a 20% boost. The best single system uses a ResNet architecture acoustic model with RNNLM rescoring, and achieves a word error rate of 6.9% on the NIST 2000 Switchboard task. The combined system has an error rate of 6.3%, representing an improvement over previously reported results on this benchmark task.

**Index Terms**— Conversational speech recognition, convolutional neural networks, recurrent neural networks, VGG, ResNet, LACE, BLSTM.

## 1. INTRODUCTION

Recent years have seen a rapid reduction in speech recognition error rates as a result of careful engineering and optimization of convolutional and recurrent neural networks. While the basic structures have been well known for a long period [1, 2, 3, 4, 5, 6, 7], it is only recently that they have emerged as the best models for speech recognition. Surprisingly, this is the case for both acoustic modeling [8, 9, 10, 11] and language modeling [12, 13]. In comparison to standard feed-forward MLPs or DNNs, these acoustic models have the ability to model a large amount of acoustic context with temporal invariance, and in the case of convolutional models, with frequency invariance as well. In language modeling, recurrent models appear to improve over classical N-gram models through the generalization ability of continuous word representations [14]. In the meantime, ensemble learning has become commonly used in several neural models [15, 16, 13], to improve robustness by reducing bias and variance.

In this paper, we use ensembles of models extensively, as well as improvements to individual component models, to advance the state-of-the-art in conversational telephone speech recognition (CTS), which has been a benchmark speech recognition task since the 1990s. The main features of this system are:

1. An ensemble of two fundamental acoustic model architectures, convolutional neural nets (CNNs) and long-short-term memory nets (LSTMs), with multiple variants of each
2. An attention mechanism in the LACE CNN which differentially weights distant context [17]
3. Lattice-free MMI training [18, 19]
4. The use of i-vector based adaptation [20] in all models

5. Language model (LM) rescoring with multiple, recurrent neural net LMs [12] running in both forward and reverse direction
6. Confusion network system combination [21] coupled with search for best system subset, as necessitated by the large number of candidate systems.

The remainder of this paper describes our system in detail. Section 2 describes the CNN and LSTM models. Section 3 describes our implementation of i-vector adaptation. Section 4 presents our lattice-free MMI training process. Language model rescoring is a significant part of our system, and described in Section 5. Experimental results are presented in Section 6, followed by a discussion of related work and conclusions.

## 2. CONVOLUTIONAL AND LSTM NEURAL NETWORKS

We use three CNN variants. The first is the VGG architecture of [22]. Compared to the networks used previously in image recognition, this network uses small (3x3) filters, is deeper, and applies up to five convolutional layers before pooling. The second network is modeled on the ResNet architecture [23], which adds a linear transform of each layer’s input to the layer’s output [24]. The only difference is that we move the Batch Normalization node to the place right before each ReLU activation.

The last CNN variant is the LACE (layer-wise context expansion with attention) model [17]. LACE is a TDNN [3] variant in which each higher layer is a weighted sum of nonlinear transformations of a window of lower layer frames. In other words, each higher layer exploits broader context than lower layers. Lower layers focus on extracting simple local patterns while higher layers extract complex patterns that cover broader contexts. Since not all frames in a window carry the same importance, an attention mask is applied. The LACE model differs from the earlier TDNN models e.g. [3, 25] in the use of a learned attention mask and ResNet like linear pass-through. As illustrated in detail in Figure 1, the model is composed of 4 blocks, each with the same architecture. Each block starts with a convolution layer with stride 2 which sub-samples the input and increases the number of channels. This layer is followed by 4 RELU-convolution layers with jump links similar to those used in ResNet. Table 1 compares the layer structure and parameters of the three CNN architectures.

While our best performing models are convolutional, the use of long short-term memory networks is a close second. We use a bidirectional architecture [26] without frame-skipping [9]. The core model structure is the LSTM defined in [8]. We found that using networks with more than six layers did not improve the word error rate on the development set, and chose 512 hidden units, per direction, per layer, as that provided a reasonable trade-off between training time and final model accuracy. Network parameters for different configurations of the LSTM architecture are summarized in Table 2.

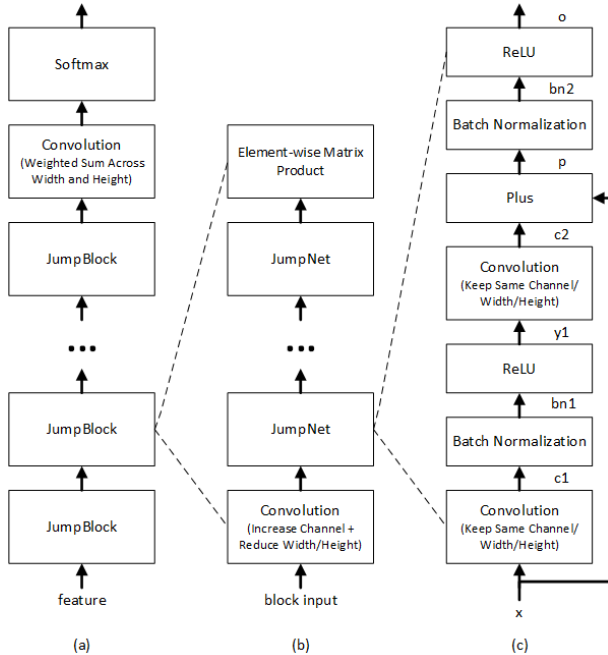


Fig. 1. LACE network architecture

### 3. SPEAKER ADAPTIVE MODELING

Speaker adaptive modeling in our system is based on conditioning the network on an i-vector [27] characterization of each speaker [20, 28]. A 100-dimensional i-vector is generated for each conversation side. For the LSTM system, the conversation-side i-vector  $v_s$  is appended to each frame of input. For convolutional networks, this approach is inappropriate because we do not expect to see spatially contiguous patterns in the input. Instead, for the CNNs, we add a learnable weight matrix  $W^l$  to each layer, and add  $W^l v_s$  to the activation of the layer before the nonlinearity. Thus, in the CNN, the i-vector essentially serves as an additional bias to each layer. Note that the i-vectors are estimated using MFCC features; by using them subsequently in systems based on log-filterbank features, we may benefit from a form of feature combination.

### 4. LATTICE-FREE SEQUENCE TRAINING

After standard cross-entropy training, we optimize the model parameters using the maximum mutual information (MMI) objective function. Denoting a word sequence by  $w$  and its corresponding acoustic realization by  $a$ , the training criterion is

$$\sum_{w, a \in \text{data}} \log \frac{P(w)P(a|w)}{\sum_{w'} P(w')P(a|w')}.$$

As noted in [29, 30], the necessary gradient for use in backpropagation is a simple function of the posterior probability of a particular acoustic model state at a given time, as computed by summing over all possible word sequences in an unconstrained manner. As first done in [18], and more recently in [19], this can be accomplished with a straightforward alpha-beta computation over the finite state acceptor representing the decoding search space. In [18], the

Table 1. Comparison of CNN architectures

VGG Net (85M Parameters)	Residual-Net (38M Parameters)	LACE (65M Parameters)
14 weight layers	49 weight layers	22 weight layers
40x41 input	40x41 input	40x61 input
3 – conv 3x3, 96	3 – [conv 1x1, 64 conv 3x3, 64 conv 1x1, 256]	5 – conv 3x3, 128
Max pool	4 – [conv 1x1, 128 conv 3x3, 128 conv 1x1, 512]	5 – conv 3x3, 256
4 – conv 3x3, 192	6 – [conv 1x1, 256 conv 3x3, 256 conv 1x1, 1024]	5 – conv 3x3, 512
Max pool	3 – [conv 1x1, 512 conv 3x3, 512 conv 1x1, 2048]	5 – conv 3x3, 1024
4 – conv 3x3, 384	Average pool	1 – conv 3x4, 1
Max pool	Softmax (9000)	Softmax (9000)
2 – FC – 4096		
Softmax (9000)		

Table 2. Bidirectional LSTM configurations

Hidden-size	Output-size	i-vectors	Depth	Parameters
512	9000	N	6	43.0M
512	9000	Y	6	43.4M
512	27000	N	6	61.4M
512	27000	Y	6	61.8M

search space is taken to be an acceptor representing the composition  $HCLG$  for a unigram language model  $L$  on words. In [19], a language model on phonemes is used instead.

In our implementation, we use a mixed-history acoustic unit language model. In this model, the probability of transitioning into a new context-dependent phonetic state (senone) is conditioned both the senone and phone history. We found this model to perform better than either purely word-based or phone-based models. Based on a set of initial experiments, we developed the following procedure:

1. Perform a forced alignment of the training data to select lexical variants and determine senone sequences.
2. Compress consecutive framewise occurrences of a single senone into a single occurrence.
3. Compute a variable-length N-gram language model from this data, where the history state consists of the previous phone and previous senones within the current phone.

To illustrate this, consider the sample senone sequence  $\{s\_s2.1288, s\_s3.1061, s\_s4.1096\}, \{eh\_s2.527, eh\_s3.128, eh\_s4.66\}, \{t\_s2.729, t\_s3.572, t\_s4.748\}$ . We would compute, e.g.,  $P(t\_s2.729|s, eh\_s2.527, eh\_s3.128, eh\_s4.66)$  and then  $P(t\_s3.572|eh, t\_s2.729)$ .

We construct the denominator graph from this language model, and HMM transition probabilities as determined by transition-counting in the senone sequences found in the training data. Our

approach not only largely reduces the complexity of building up the language model but also provides very reliable training performance.

We have found it convenient to do the full computation, without pruning, in a series of matrix-vector operations on the GPU. The underlying acceptor is represented with a sparse matrix, and we maintain a dense likelihood vector for each time frame. The alpha and beta recursions are implemented with CUSPARSE level-2 routines: sparse-matrix, dense vector multiplies. Run time is about 100 times faster than real time. As in [19], we use cross-entropy regularization. In all the lattice-free MMI (LFMMI) experiments mentioned below we use a trigram language model. Most of the gain is usually obtained after processing 24 to 48 hours of data.

## 5. LM RESCORING AND SYSTEM COMBINATION

An initial decoding is done with a WFST decoder, using the architecture described in [31]. We use an N-gram language model trained and pruned with the SRILM toolkit [32]. The first-pass LM has approximately 15.9 million bigrams, trigrams, and 4grams, and a vocabulary of 30500 words. and gives a perplexity of 54 on RT-03 speech transcripts. The initial decoding produces a lattice with the pronunciation variants marked, from which 500-best lists are generated for rescoring purposes. Subsequent N-best rescoring uses an unpruned LM comprising 145 million N-grams. All N-gram LMs were estimated by a maximum entropy criterion as described in [33].

### 5.1. RNNLM setup

The N-best hypotheses are then rescored using a combination of the large N-gram LM and several RNNLMs, trained and evaluated using the CUED-RNNLM toolkit [34]. Our RNNLM configuration has several distinctive features:

- We trained both standard, forward-predicting RNNLMs and backward RNNLMs that predict words in reverse temporal order. The log probabilities from both models are added.
- As is customary, the RNNLM probability estimates are interpolated at the word-level with corresponding N-gram LM probabilities (separately for the forward and backward models). In addition, we trained a second RNNLM for each direction, obtained by starting with different random initial weights. The two RNNLMs and the N-gram LM for each direction are interpolated with weights of (0.375, 0.375, 0.25).
- In order to make use of LM training data that is not fully matched to the target conversational speech domain, we start RNNLM training with the union of in-domain (here, CTS) and out-of-domain (e.g., Web) data. Upon convergence, the network undergoes a second training phase using the in-domain data only. Both training phases use in-domain validation data to regulate the learning rate schedule and termination.
- We found best results with an RNNLM configuration that had a second, non-recurrent hidden layer. This produced lower perplexity and word error than the standard, single-hidden-layer RNNLM architecture [12].<sup>1</sup> The overall network architecture thus had two hidden layers with 1000 units each, using ReLU nonlinearities. Training used noise-contrastive estimation (NCE) [35].

<sup>1</sup>However, adding more hidden layers produced no further gains.

**Table 3.** Performance of various versions of RNNLM rescoring. Perplexities (PPL) are computed on 2001 CTS eval transcripts; word error rates (WER) on the NIST 2000 Switchboard test set.

Language model	PPL	WER
4-gram LM (baseline)	75.5	9.6
+ RNNLM, CTS data only	63.2	9.2
+ Web data training	61.9	8.9
+ 2nd hidden layer	59.8	8.8
+ backward RNNLM	-	8.6
+ 2-RNNLM interpolation	57.4	8.5

- The RNNLM output vocabulary consists of all words occurring in the in-domain training set. For rescoring purposes the number of out-of-set words is recorded for each hypothesis and a penalty for them is empirically estimated, along with the weights for the LM score proper and the pronunciation probabilities, using the SRILM *nbest-optimize* tool.

### 5.2. Training data

The 4-gram language model for decoding was trained on the available CTS transcripts from the DARPA EARS program: Switchboard (3M words), BBN Switchboard-2 transcripts (850k), Fisher (21M), English CallHome (200k), and the University of Washington conversational Web corpus (191M). A separate model was trained from each source and interpolated with weights optimized on RT-03 transcripts. For the unpruned large rescoring 4-gram, an additional LM component was added, trained on 133M word of LDC Broadcast News texts. The N-gram LM configuration is modeled after that described in [28], except that maxent smoothing was used.

The RNNLMs were trained on Switchboard and Fisher transcripts as in-domain data (20M words for gradient computation, 3M for validation). To this we added 62M words of UW Web data as out-of-domain data, for use in the two-phase training procedure described above.

### 5.3. RNNLM performance

Table 3 gives perplexity and word error performance for various RNNLM setups, from simple to more complex. The acoustic model used was a preliminary CNN.

As can be seen, each of the measures described earlier adds incremental gains, which, while small individually, add up to a 14% relative reduction in word error.

### 5.4. System Combination

The LM rescoring is carried out separately for each acoustic model. The rescored N-best lists from each subsystem are then aligned into a single confusion network [21] using the SRILM *nbest-rover* tool. However, the number of potential candidate systems is too large to allow an all-out combination, both for practical reasons and due to overfitting issues. Instead, we perform a greedy search, starting with the single best system, and successively adding additional systems, to find a small set of systems that are maximally complementary. The RT-02 Switchboard set was used for this search procedure. Once a good subset of systems is found, their relative weighting (for confusion-network mediated voting) is optimized using an EM algorithm, again using the development set.

## 6. EXPERIMENTAL SETUP AND RESULTS

### 6.1. Speech corpora

We train with the commonly used English CTS (Switchboard and Fisher) corpora. Evaluation is carried out on the NIST 2000 CTS test set, which comprises both Switchboard (SWB) and CallHome (CH) subsets. The Switchboard-1 portion of the NIST 2002 CTS test set was used for tuning and development. The acoustic training data is comprised by LDC corpora 97S62, 2004S13, 2005S13, 2004S11 and 2004S09; see [18] for a full description.

### 6.2. 1-bit SGD Training

All presented models are costly to train. To make training feasible, we parallelize training with our previously proposed 1-bit SGD parallelization technique [36]. This data-parallel method distributes minibatches over multiple worker nodes, and then aggregates the sub-gradients. While the necessary communication time would otherwise be prohibitive, the 1-bit SGD method eliminates the bottleneck by two techniques: *1-bit quantization of gradients* and *automatic minibatch-size scaling*.

In [36], we showed that gradient values can be quantized to just a single bit, if one carries over the quantization error from one minibatch to the next. Each time a sub-gradient is quantized, the quantization error is computed and remembered, and then added to the next minibatch’s sub-gradient. This reduces the required bandwidth 32-fold with minimal loss in accuracy. Secondly, automatic minibatch-size scaling progressively decreases the frequency of model updates. At regular intervals (e.g. every 72h of training data), the trainer tries larger minibatch sizes on a small subset of data and picks the largest that maintains training loss.

### 6.3. Acoustic Model Details

Forty-dimensional log-filterbank features were extracted every 10 milliseconds, using a 25-millisecond analysis window. The CNN models used window sizes as indicated in Figure 1, and the LSTMs processed one frame of input at a time. The bulk of our models use three state left-to-right triphone models with 9000 tied states. Additionally, we have trained several models with 27k tied states. The phonetic inventory includes special models for noise, vocalized-noise, laughter and silence. We use a 30k-vocabulary derived from the most common words in the Switchboard and Fisher corpora. The decoder uses a statically compiled unigram graph, and dynamically applies the language model score. The unigram graph has about 300k states and 500k arcs. All acoustic models were trained using the open-source Computational Network Toolkit (CNTK) [37].

Table 4 shows the result of i-vector adaptation and LFMFI training on several of our systems. We achieve a 5–8% relative improvement from i-vectors, including on CNN systems. The last row of Table 4 shows the effect of LFMFI training on the different models. We see a consistent 7–10% further relative reduction in error rate for all models. Considering the great increase in procedural simplicity of LFMFI over the previous practice of writing lattices and post-processing them, we consider LFMFI to be a significant advance in technology.

### 6.4. Comparative System Performance

Model performance for our individual models as well as relevant comparisons from the literature are shown in Table 5. Out of the 15 models built, only models given non-zero weight in the final system combination are shown.

**Table 4.** Performance improvements from i-vector and LFMFI training on the eval 2000 set.

Configuration	WER (%)					
	ReLU-DNN		BLSTM		LACE	
	CH	SWB	CH	SWB	CH	SWB
Baseline	21.9	13.4	17.3	10.3	16.9	10.4
i-vector	20.1	11.5	17.6	9.9	16.4	9.3
i-vector+LFMFI	17.9	10.2	16.3	8.9	15.2	8.5

**Table 5.** Word error rates (%) on the eval 2000 set with different acoustic models. Unless otherwise noted, models are trained on the full 2000 hrs. of data and have 9k senones.

Model	N-gram LM		RNN LM	
	CH	SWB	CH	SWB
Saon et al. [28] LSTM	15.1	9.0	-	-
Povey et al. [19] LSTM	15.3	8.5	-	-
Saon et al. [28] Combination	-	-	12.2	6.6
300h ResNet	19.2	10.0	17.7	8.2
ResNet GMM alignment	15.3	8.8	13.7	7.3
ResNet	14.8	8.6	13.2	6.9
VGG	15.7	9.1	14.1	7.6
LACE	14.8	8.3	13.5	7.1
BLSTM	16.7	9.0	15.3	7.8
27k Senone BLSTM	16.2	8.7	14.6	7.5
Combination	13.4	7.4	<b>11.9</b>	<b>6.3</b>

## 7. RELATION TO PRIOR WORK

Compared to earlier applications of CNNs to speech recognition [38, 39], our networks are much deeper, and use linear bypass connections across convolutional layers. They are similar in spirit to those studied more recently by [11, 10, 28]. We improve on these architectures with the LACE model [17], which iteratively expands the effective window size, layer-by-layer, and adds an attention mask to differentially weight distant context. Our use of lattice-free MMI is distinctive, and extends previous work [18, 19] by proposing the use of a mixed triphone/phoneme history in the language model.

On the language modeling side, we achieve a performance boost by combining multiple RNNLMs in both forward and backward directions, and by using a two-phase training regimen to get best results from out-of-domain data. For our best CNN system, RNNLM rescoring yields a relative word error reduction of 18%, and a 15% relative gain for the combined recognition system.

## 8. CONCLUSIONS

We have described Microsoft’s conversational speech recognition system for 2016. The use of CNNs in the acoustic model has proved singularly effective, as has the use of RNN language models. Our best single system achieves an error rate of 6.9% on the NIST 2000 Switchboard set. We believe this is the best performance reported to date for a recognition system not based on system combination. An ensemble of acoustic models advances the state of the art to 6.3% on the Switchboard test data.

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